

Ordering properties

Compare the given real numbers.

$$\begin{aligned}\frac{1}{3} < \frac{1}{6} &\Leftrightarrow \frac{1}{3} + \left(-\frac{1}{6}\right) < \frac{1}{6} + \left(-\frac{1}{6}\right) \\ &\Leftrightarrow \frac{1}{3} - \frac{1}{6} < 0 \\ &\Leftrightarrow \frac{6-3}{18} < 0 \quad \text{False.}\end{aligned}$$

$$\begin{aligned}-5 + (-(-6)) &= -5 + 6 = 1 > 0 \\ -5 + (-(-6)) + (-6) &> 0 + (-6) \\ -5 &> -6. \quad \text{True.}\end{aligned}$$

$$\begin{aligned}-3 < -\frac{3}{2} &\Leftrightarrow (-2)(-3) > (-2)\left(-\frac{3}{2}\right) \\ &\Leftrightarrow 6 > 3 \quad \text{True}\end{aligned}$$

$$\sqrt{2} < \sqrt{4} = 2. \quad \text{and} \quad 2 < 200$$

$$\sqrt{2} < 200.$$

then

$a, b \in \mathbb{R}$: Either $a < b$, or
 $a = b$, or
 $a > b$.

$$a \leq b \Leftrightarrow (a < b \text{ or } a = b)$$

$$a < b \Leftrightarrow a + c < b + c.$$

$$a < b \Leftrightarrow \begin{cases} ac < bc & \text{if } c > 0 \\ ac > bc & \text{if } c < 0. \end{cases}$$

$$a < b \text{ and } b < c \Rightarrow a < c.$$

$$\frac{1}{3} \text{ and } \frac{1}{6}.$$

$$\text{So } \frac{1}{3} > \frac{1}{6}.$$

$$-5 \text{ and } -6$$

$\Leftrightarrow$

$\Leftrightarrow$

$$-3 \text{ and } -\frac{3}{2}$$

$$\text{So } -3 < -\frac{3}{2}.$$

$$\sqrt{2} \text{ and } 200.$$

$$2.7331 \text{ and } 2.733$$

$$2.7331 = 2.733 + 0.0001 > 2.733.$$