

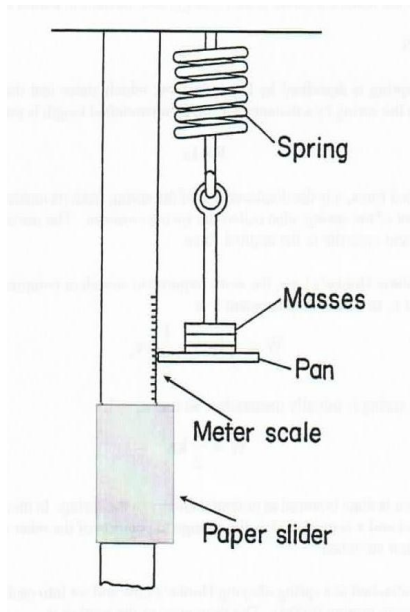
Physics 1D03: Lab 2

HOOKE'S LAW

Lab Objectives

- Understand the theory behind Hooke's Law and the physics behind springs.
- Experimentally determine a spring constant through Hooke's Law, Conservation of Energy, and measuring period.
- Learn more about Excel and calculating functions.
- Justify the spring constant and springs mass with theoretical predictions.
- Working with uncertainties when recording measurements.

Equipment



Spring-Mass system



Stop-Watch

Part 1: Force vs. Displacement

Part 1: Force vs. Displacement

- Goal is to first find the spring constant, k , and no-load position of the spring, x_0
- Place the metal pan (*without any additional masses*) on the spring
 - Refer to image for an example of the set-up
- Using the ruler, measure the position of the bottom edge of the pan
 - Record this value in your report



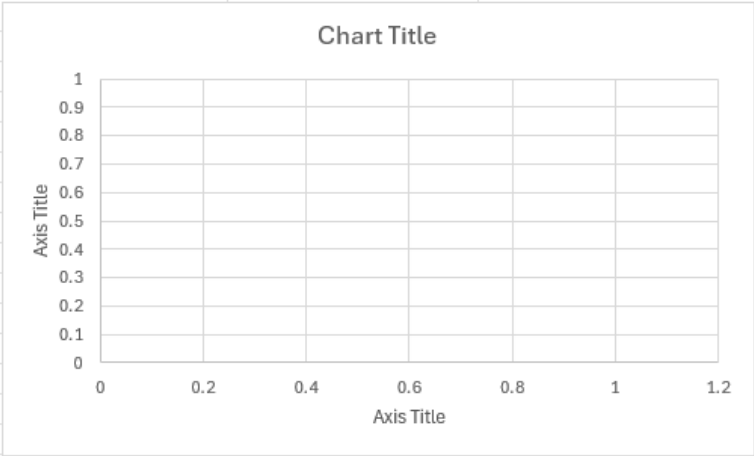
Part 1: Force vs. Displacement

- After taking the measurement, add a 20gm mass to the pan and record the new position (include an uncertainty measurement)
 - Note: Do **not** measure the difference of position, just record only the values you see on the ruler
 - Record this value in your report
- Add another 20gm mass and repeat the above steps until you have a total of 10 measurements
- We can now use Excel to plot our results



Part 1: Force vs. Displacement

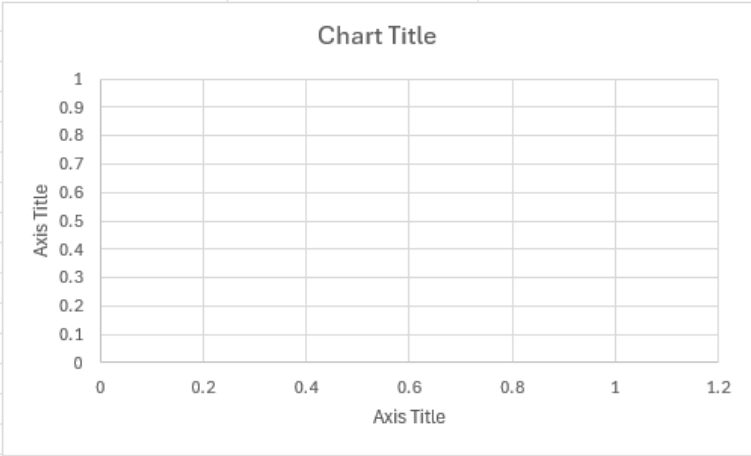
| Mass (kg) | Mass Uncertainty (kg) | Load (kg*m/s ²) | Load Uncertainty (kg*m/s ²) | Pan Position (m) |
|-------------|-------------------------|------------------------------|--|--------------------|
| | 0 | 0 | 0 | 0 |
| | 0 | 0 | 0 | 0 |
| | 0 | 0 | 0 | 0 |
| | 0 | 0 | 0 | 0 |
| | 0 | 0 | 0 | 0 |
| | 0 | 0 | 0 | 0 |
| | 0 | 0 | 0 | 0 |
| | 0 | 0 | 0 | 0 |
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Input data in these boxed
(Note what units you should
be entering the data in)

Part 1: Force vs. Displacement

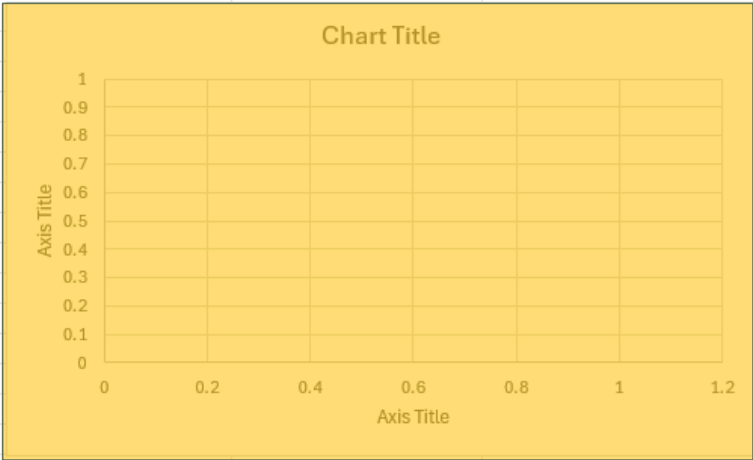
| Mass (kg) | Mass Uncertainty (kg) | Load (kg*m/s^2) | Load Uncertainty (kg*m/s^2) | Pan Position (m) |
|-------------|-------------------------|-------------------|-------------------------------|--------------------|
| | 0 | 0 | 0 | |
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| | 0 | 0 | 0 | |



These cells will automatically be calculated for you

Part 1: Force vs. Displacement

| Mass (kg) | Mass Uncertainty (kg) | Load (kg*m/s^2) | Load Uncertainty (kg*m/s^2) | Pan Position (m) |
|-------------|-------------------------|-------------------|-------------------------------|--------------------|
| | 0 | 0 | 0 | |
| | 0 | 0 | 0 | |
| | 0 | 0 | 0 | |
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| | 0 | 0 | 0 | |
| | 0 | 0 | 0 | |
| | 0 | 0 | 0 | |
| | 0 | 0 | 0 | |



Plot for 'mg' vs. 'Position of Pan' appears here
(Remember to label/rescale)

Part 1: Force vs. Displacement

- Copy data from Excel sheet into your lab report
- Generate a line of best fit on your Excel graph and use that to find the spring constant, k , and no-load position of the spring, x_0
 - Hint: Consider how your line of best fit is related to Hooke's Law

$$F = k\Delta x$$

where Δx is the displacement from the no-load position. What would F be in this case?



Part 2: Energy vs Displacement

Part 2: Energy vs. Displacement

- We now want to measure the potential energy of the spring using the displacement of the mass
- Energy conservation tells us that the energy before/after the mass is dropped is given by

$$mgh = \frac{1}{2}kx^2$$

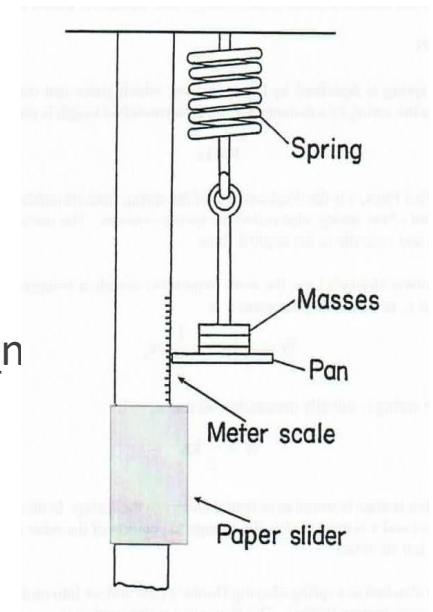
which can be rewritten as

$$\log(mh) = 2 \log(h) + \text{constant}$$

- This equation is what we will use to test energy conservation

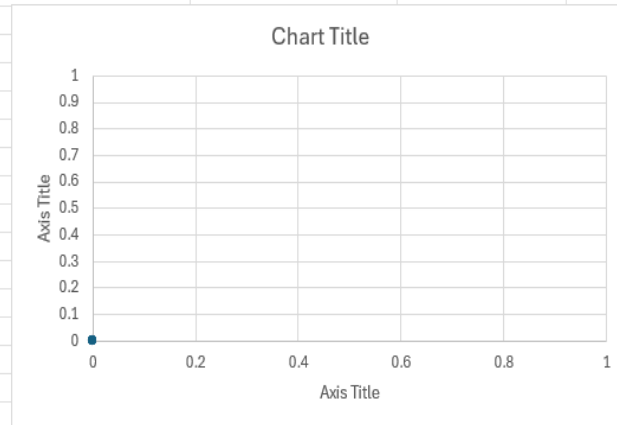
Part 2: Energy vs. Displacement

- Start by moving the empty pan up to the no-load position, x_0 , measured from Part 1
- Place the paper slider directly below the pan and record its position in the report
- Release the pan, allowing the slider be pushed down
 - Record the mass of the pan and new slider **position (not the displacement)** in your report and Excel file
- Repeat the above steps 5-6 more times, adding an additional 20gm to the pan each time
- We can now use the data to plot $\log(mh)$ vs. $\log(h)$



Part 2: Energy vs. Displacement

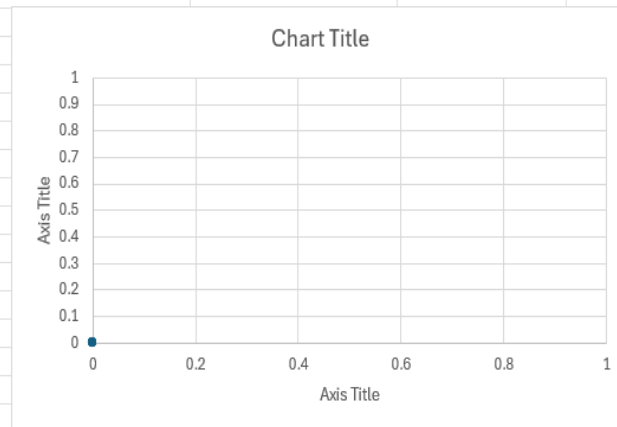
| | | | | | | | | |
|-----------------------------|---------------------------------|------------------------------|-------------------------------|-------------------|----------------------------------|-----------------------|--------------------------------------|--|
| Uncertainty in height (m) = | | <- record uncertainty in B1 | | | | | | |
| xo (m) = | | <- record xo in B2 | | | | | | |
| Mass (kg) | Uncertainty in mass (kg) | Position of paper (m) | Change in height h (m) | log(h) (m) | Uncertainty in log(h) (m) | log(mh) (kg*m) | Uncertainty in log(mh) (kg*m) | |
| | | 0 | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! | |
| | | 0 | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! | |
| | | 0 | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! | |
| | | 0 | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! | |
| | | 0 | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! | |
| | | 0 | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! | |



Input data in these boxed

Part 2: Energy vs. Displacement

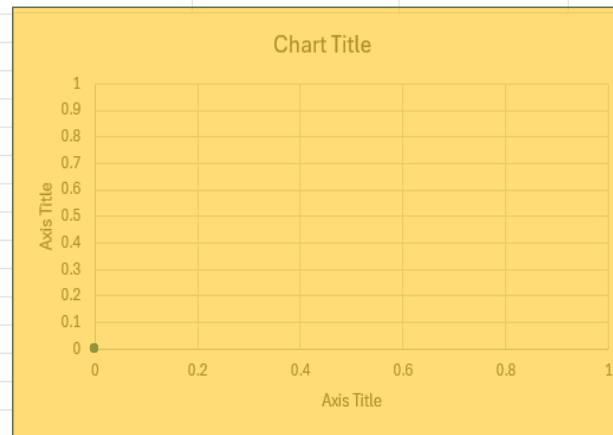
| Uncertainty in height (m) = | | <- record uncertainty in B1 | | | | | |
|-----------------------------|--------------------------|-----------------------------|------------------------|------------|---------------------------|----------------|-------------------------------|
| xo (m) = | | <- record xo in B2 | | | | | |
| Mass (kg) | Uncertainty in mass (kg) | Position of paper (m) | Change in height h (m) | log(h) (m) | Uncertainty in log(h) (m) | log(mh) (kg*m) | Uncertainty in log(mh) (kg*m) |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
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| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |



Results will automatically be calculated here

Part 2: Energy vs. Displacement

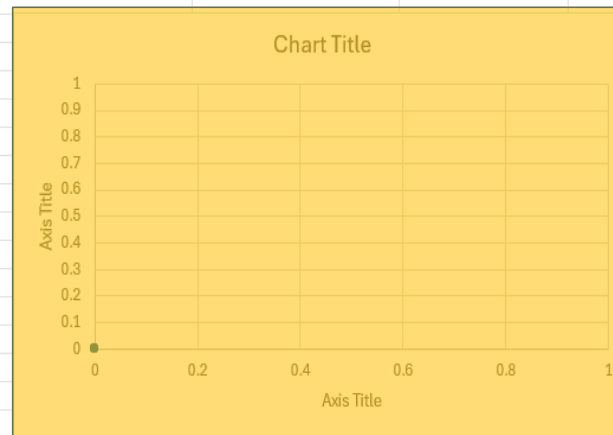
| Uncertainty in height (m) = | | <- record uncertainty in B1 | | | | | |
|-----------------------------|--------------------------|-----------------------------|------------------------|------------|---------------------------|----------------|-------------------------------|
| xo (m) = | | <- record xo in B2 | | | | | |
| Mass (kg) | Uncertainty in mass (kg) | Position of paper (m) | Change in height h (m) | log(h) (m) | Uncertainty in log(h) (m) | log(mh) (kg*m) | Uncertainty in log(mh) (kg*m) |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |



Plot for 'log(mh)' vs. 'log(h)'
appears here
(Remember to label/rescale)

Part 2: Energy vs. Displacement

| Uncertainty in height (m) = | <- record uncertainty in B1 | | | | | | |
|-----------------------------|-----------------------------|-----------------------|------------------------|------------|---------------------------|----------------|-------------------------------|
| xo (m) = | <- record xo in B2 | | | | | | |
| Mass (kg) | Uncertainty in mass (kg) | Position of paper (m) | Change in height h (m) | log(h) (m) | Uncertainty in log(h) (m) | log(mh) (kg*m) | Uncertainty in log(mh) (kg*m) |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |
| | 0 | | 0 | #NUM! | #DIV/0! | #NUM! | #DIV/0! |



Include a line of best fit, then use that to answer the provided discussion questions.

Remember to copy all the data into your lab report!

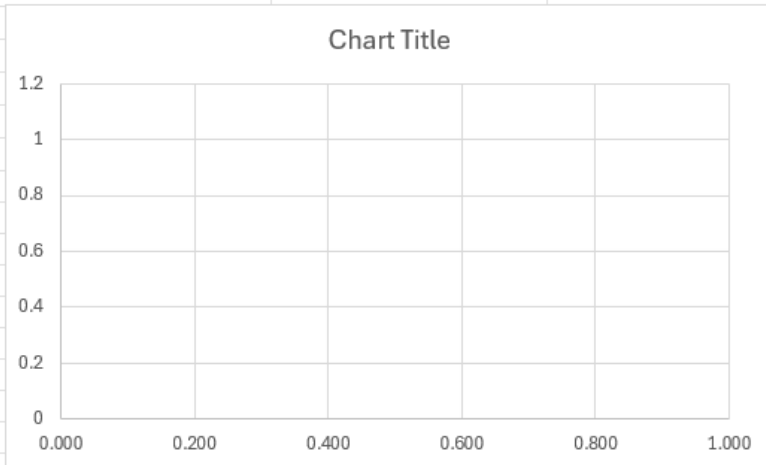
Part 3: Mass vs. Natural Frequency

Part 3: Mass vs. Natural Frequency

- Here we want to measure the “*effective spring mass*”, m_0
- Starting with 50gm mass, drop the pan from an initial starting position
- Record the time it takes to complete 50 oscillations
 - Record this value in your Excel file/report
- Repeat 4 more times using 60gm, 70gm, 90gm, and 110gm masses
- We can now use Excel to plot the mass as a function of T^2

Part 3: Mass vs. Natural Frequency

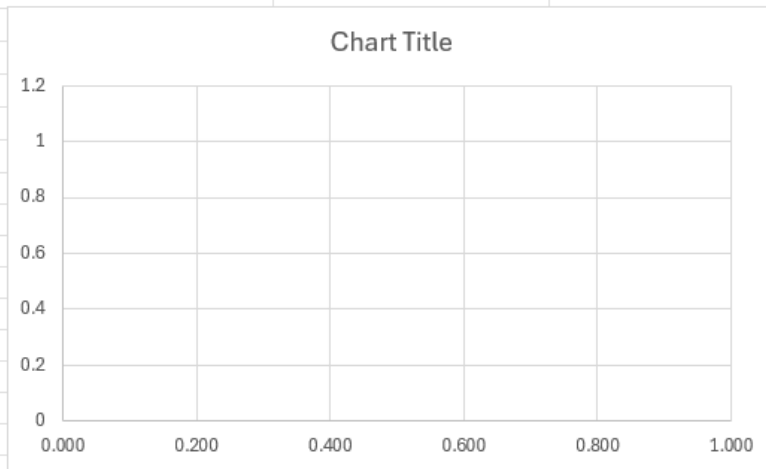
| Uncertainty of time (s) | Number of swings n | Error in Period (s) | | | | |
|-------------------------|----------------------------|--------------------------|--------------|-----------------------------------|--|--|
| | 50 | 0 | | | | |
| | | | | | | |
| | | | | | | |
| Mass (kg) | Uncertainty in mass (kg) | Time for 50 swings (s) | Period (s) | Period squared (s ²) | Error in Period Squared (s ²) | |
| | 0 | | 0.000 | 0.000 | 0.000 | |
| | 0 | | 0.000 | 0.000 | 0.000 | |
| | 0 | | 0.000 | 0.000 | 0.000 | |
| | 0 | | 0.000 | 0.000 | 0.000 | |
| | 0 | | 0.000 | 0.000 | 0.000 | |



Input data in these boxed

Part 3: Mass vs. Natural Frequency

| Uncertainty of time (s) | Number of swings n | Error in Period (s) | | | | |
|-------------------------|----------------------------|--------------------------|--------------|-----------------------------------|--|--|
| | 50 | 0 | | | | |
| | | | | | | |
| | | | | | | |
| Mass (kg) | Uncertainty in mass (kg) | Time for 50 swings (s) | Period (s) | Period squared (s ²) | Error in Period Squared (s ²) | |
| | 0 | | 0.000 | 0.000 | 0.000 | |
| | 0 | | 0.000 | 0.000 | 0.000 | |
| | 0 | | 0.000 | 0.000 | 0.000 | |
| | 0 | | 0.000 | 0.000 | 0.000 | |
| | 0 | | 0.000 | 0.000 | 0.000 | |



Results will automatically be calculated here

Part 3: Mass vs. Natural Frequency

| Uncertainty of time (s) | Number of swings n | Error in Period (s) | | | | | | | |
|-------------------------|----------------------------|--------------------------|--------------|-----------------------------------|--|--|--|--|--|
| | 50 | 0 | | | | | | | |
| | | | | | | | | | |
| | | | | | | | | | |
| Mass (kg) | Uncertainty in mass (kg) | Time for 50 swings (s) | Period (s) | Period squared (s ²) | Error in Period Squared (s ²) | | | | |
| | 0 | | 0.000 | 0.000 | 0.000 | | | | |
| | 0 | | 0.000 | 0.000 | 0.000 | | | | |
| | 0 | | 0.000 | 0.000 | 0.000 | | | | |
| | 0 | | 0.000 | 0.000 | 0.000 | | | | |
| | 0 | | 0.000 | 0.000 | 0.000 | | | | |



Plot for 'Mass' vs. 'Period²'
appears here
(Remember to label/rescale)

Part 3: Mass vs. Natural Frequency

- Copy data from Excel sheet into your lab report
- Generate a line of best fit on your Excel graph and use that to find the effective spring mass, m_0
 - Hint: Since you are plotting m vs. T^2 , compare your line of best fit to the equation

$$m = -m_0 + \frac{kT^2}{4\pi^2}$$

Good Luck!