# Physics 1D03: Lab 1

SIMPLE AND PHYSICAL PENDULUMS

Updated: Apr. 29, 2024

### Lab Objectives

- Understand the theory behind a simple and physical pendulum.
- Determine uncertainties in the lab and propagate uncertainties for multivariable equations.
- Expose oneself to Microsoft Excel and spreadsheet software.
- Experimentally determine the period of a simple pendulum with a variable length and angle.
- Justify the experimental results of the simple pendulum with theoretical predictions through the analysis of the gravitational constant g.
- Experimentally examine the behavior of a physical pendulum with Capstone software.

### Equipment



Physical Pendulum using PASCO Capstone Software



Simple Pendulum (heavy mass on string)



Stop-Watch, protractor, and ruler

## Part 1: The Simple Pendulum Part A

#### Part A: Preliminary Study

• We first want to understand what the uncertainties in our experiment are

Start by setting the length of the pendulum to 10cm

•You and a partner will take turns releasing the pendulum and timing how long it takes for the mass to swing 1, 5, and 10 times

Record the times and period in your report with uncertainties

Make sure to have a TA come and check your answers

 How do you think the uncertainty in your recorded time relates to the uncertainty of a single swing?



## Part 1: The Simple Pendulum Part B

- We now want to see how changing the amplitude of the pendulum affects the period
- Pick a convenient length to set the pendulum at to measure 10 swings
- Measure the time for a small amplitude (~5<sup>o</sup>) and record your results
  - Repeat for 5 more angles varying between  $5^o$  and  $60^o$
- Using Excel, you can plot the results for T vs.  $\theta$



ror in time for 10 Swings (s) Error in Period & T (s)	0 Period ( )						
	0						
	0						
	0						
	0						
	0						
	1		Т	itle			
	0.9						
	.0.8						_
	0.7	-					
Input data in these boyed	9.0 <u>H</u>						
input data in triese boxed	5 0.5						
	0.3						
	0.2						
	0.1						
	0						
		0 0.	2 0.4	0.6 Axis Title	0.8	1	1.2

Amplitude (degrees)	Time for 10 Swings ( )	0 Period ( ) 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0							
		0							
Results will calcu	automatically be lated here		1 0.9 0.8 0.7 0.5 0.5 0.4						
			0.3 0.2 0.1 0 0	0.2	0.4	0.6 Axis Title	0.8	1	1.2

plitude (degrees)	T' ( 10 C ' ( )	D 11()					
	Time for 10 Swings ()	Period ( )					
		0					
		0					
		0					
		0					
		0					
					 tie		
			1 _				
			0.9				_
		-	0.8				
			0.7				
Plot a	appears here						
	ure to properly		XX 0.4				
(Make s			0.3				
(Make s	a vave elat than					 	
(Make s label/scal	e your plot, then		0.2 -				
(Make s label/scal copy-paste	e your plot, then it into your report)		0.2				
(Make s label/scal copy-paste	e your plot, then it into your report)		0.2 0.1 0 -	,		 	_

## Part 1: The Simple Pendulum Part C

 Goal is to calculate the gravitational constant g using two methods

#### Method 1)

- Select a convenient angle to swing the pendulum
- Set the length of the string to 10cm and measure the time for 10 swings
  - Record your results and calculate the period
  - Repeat for 4 more evenly spaced lengths (for a total of 5), varying between 10cm and 80cm



Calculate T<sup>2</sup> (period squared) and g (gravitational constant) only using the first set of measurements (ie. only the data from the 10cm run)

$$g = \frac{4\pi^2 l}{T^2}$$

- Then find the equations that calculate the uncertainties for the period squared and gravitational constant ,  $\delta(T^2)$  and  $\delta(g)$ 
  - Remember to use your error propagation rules here!
- Use these equations to calculate the uncertainties in  $T^2$  and g again using the first set of measurements only

We can now use Excel to compare our answer

<u>Error in length (cm)</u>	Error for T	ime of 10 swings (s)	]	Error in Period ôT (s)							
					_						
Length <i>l</i> (cm)	Time for 10	) swings (s)	]	Period T (s)	Period Square	ed T^2 (s^2)	Error in T^2 (s^2)		Gravitational constant $g$ (m/s <sup>2</sup> )	Error in Gravitat	ional constant δg (m/s^2)
				(			0	0	#DIV/0!		#DIV/0!
				(			0	0	#DIV/0!		#DIV/0!
				(			0	0	#DIV/0!		#DIV/0!
				(	)		0	0	#DIV/0!		#DIV/0!
				(	)		0	0	#DIV/0!		#DIV/0!
									Average g:	Average δg:	
				Chart Title					#DIV/0!		#DIV/0!
				onare nero							
	0.9										
	0.8										
	0.7										
	0.6 س										1
	E 0.5										
	¥ 0.4										
	0.3								Input data in these	boxed	
	0.0										
	0.2										
	0.1										
	0	0.2	0.4	0.0	0.0	4	-				
	U	0.2	0.4	U.b Avis Titlo	0.8	T	1.2				
				AXIS TITLE							

Error in length (cm)	Error for Time of 10 swings (s)	Error in Period ôT (s)						
Length <i>l</i> (cm)	Time for 10 swings (s)	Period T (s)	Period Squared T^2 (s^2)	Error in T^2 (s^2)		Gravitational constant g (m/s^2)	Error in Gravitat	tional constant ôg (m/s^2)
			0 0 0	0 0 0	( ( (	#DIV/0! #DIV/0! #DIV/0!		#DIV/0! #DIV/0! #DIV/0!
			0	0	(	#DIV/0! #DIV/0!		#DIV/0! #DIV/0!
		Chart Title				Average g: #DIV/0!	Average δg:	#DIV/0!
	0.9							
	0.7 0.7 0.6 U.5 0.5 0.4 0.3 0.2 0.1				I	Results will automat calculated her	ically be re	
	0 0.2	0.4 0.6 Axis Title	0.8 1	1.2				

Error in length (cm)	Error for Time of 10 swings (s)	Error in Period ôT (s)					
Length <i>l</i> (cm)	Time for 10 swings (s)	Period T (s)	Period Squared T^2 (s^2)	Error in T	^2 (s^2)	Gravitational constant g (m	/s^2) Error in Gravitational constant ôg (m/s^2)
			0	0		0 #DIV/0!	#DIV/0!
			0	0		0 #DIV/0!	#DIV/0!
			0	0		0 #DIV/0!	#DIV/0!
			0	0		0 #DIV/0!	#DIV/0!
			0	0		0 #DIV/0!	#DIV/0!
						Average g:	Average δg:
		Chart Title				#DIV/0!	#DIV/0!
	0.9 0.8 0.7 0.6 0.5 0.5 0.4 0.3 0.2 0.1				**Before for the un Have a TA	<u>continuing, mak</u> certainties agree come and check moving f	<u>e sure your calculations</u> <u>e with what Excel has!**</u> c your calculations before orward
	0 0.2	0.4 0.6	0.8 1	12		- 0	

Error in length (cm)	Error for Time of 10 swings (s)	Error in Period ôT (s)				
Length <i>l</i> (cm)	Time for 10 swings (s)	Period T (s)	Period Squared T^2 (s^2)	Error in T^2 (s^2)	Gravitational constant $g$ (m/s <sup>2</sup> )	Error in Gravitational constant ôg (m/s^2)
			0	0	0 #DIV/0!	#DIV/0!
			0	0	0 #DIV/0!	#DIV/0!
			0	0	0 #DIV/0!	#DIV/0!
			0	0	0 #DIV/0!	#DIV/0!
			0	0	0 #DIV/0!	#DIV/0!
					Average g:	Average δg:
		Chart Title			#DIV/0!	#DIV/0!
	0.9 0.8 0.7 0.6 0.5 0.4 0.4 0.3 0.2 0.1 0 0 0.2	0.4 0.6 Axis Title	0.8 1	This averag gravitation this	e value of <i>g</i> is how al constant from our <i>g</i> and its uncertainty	we will determine the r first method. Record r, in the report.

• We can also calculate g using another approach

#### Method 2)

- Based off the collected data, we can plot the results on a " $T^2$  vs. length" graph and examine the line of best fit
- The Excel spreadsheet will automatically make the plot once you enter all your data
  - You will need to include a trendline for your graph
  - Instructions for doing so will be on the manual

Error in length (cm)	Error for Time of 10 swings	(s) Error in Period ôT (s)						
Length <i>l</i> (cm)	Time for 10 swings (s)	Period T (s)	Period Squared T^2 (s^2)	Error in T^2 (s^2)		Gravitational constant $g$ (m/s^2)	Error in Grav	ritational constant ôg (m/s^2)
			0	0	0	#DIV/0!		#DIV/0!
			0	0	0	#DIV/0!		#DIV/0!
			0	0	0	#DIV/0!		#DIV/0!
			0	0	0	#DIV/0!		#DIV/0!
			0	0	0	#DIV/0!		#DIV/0!
						Average g	Average δg:	
		Chart Tala				#DIV/0!	The age og	#DIV/0!
		Chart Htle						
	- 1			—				
	0.9							
	0.8							]
	0.7							
	u 0.6			_	D	Not for $T^2$ vs. length	will	
	Ē 0.5					lot lot 1 v3. lengti	vviii	
	AXis					appear here		
	0.4				/D			
	0.3				(Pro	perly label/scale yo	our plot,	
	0.2				the	en conv-naste it inte	o vour	
	0.1			_			your	
	0			_		report)		
	0 0.2	0.4 0.6	0.8 1	1.2		• •		
		Axis Title						

The trendline would give you an equation of the form

 $T^2 = ml + b$ 

Where m is the slope and b is the intercept

Comparing with the equation

$$T^2 = \frac{4\pi^2}{g}l$$

We see that

slope for line of best fit = 
$$\frac{4\pi^2}{g}$$

Solving for g this way will give us another way to find the gravitational constant

20

- First check the pendulum bar is attached to the sensor using the hole at the end (see picture)
- Open the PASCO software on the desktop and create an "Angle (rad) vs. Time" plot
- •Measure an angle of 15<sup>o</sup> with the pendulum and start recording
- Release the pendulum and let it swing at least 15 times



- Using the PASCO software, find the time it took the pendulum to oscillate 10 times
- Calculate the period and record the results in your report
   with uncertainties
  - Hint: Would your uncertainties be the same in this case? What was causing the uncertainty in Part 1 of the experiment and is it the same here?
- Once done, move to the next hole of the pendulum bar and repeat the previous steps (see picture) for a total of 7 runs



Error in time ( )	Error in Period ôT ( )	Length ( )	Distance between holes ( )							
			<inp< th=""><th>put data here</th><th>e, and distan</th><th>ce to centre of</th><th>mass will a</th><th>utomatically be</th><th>filled</th><th></th></inp<>	put data here	e, and distan	ce to centre of	mass will a	utomatically be	filled	
n	Distance to centre of mass ( )	Time for 10 swings ( )	Period T ( )							
0	0		0							
1	0		0							
2	0		0							
3	0		0							
4	0		0							
5	0		0				Chart T	itla		_
6	0		0				chart i	itie		_
				1						
				0.9	,					-
				0.8						
										-
				0.7						
		-		음 <sup>0.6</sup>	;					
				Ē 0.5	;					
	Input data in th	lese boxed		- Ž 0.4	. —					
				0.5	'					
				0.2	2					
				0.1						
				0	) 🖕			1		
					0	0.2	0.4	0.6	0.8	1
							Axis	Title		

Error in time ( )	Error in Period ôT ( )	Length ( )	Distance between holes ( )	)						
				<input data="" h<="" th=""/> <th>ere, and dis</th> <th>stance to centre o</th> <th>of mass will au</th> <th>tomatically be</th> <th>filled</th> <th></th>	ere, and dis	stance to centre o	of mass will au	tomatically be	filled	
n	Distance to centre of mass ( )	Time for 10 swings ( )	Period T ( )	-						
	0		C							
1	. 0		0							
2	0		0							
3	0		0							
4	0		0							
6	0 0		0				Chart Ti	tle		_
				2 						
					0.8					
					0.7					
	Results will auto	matically be		Title	0.6					
	calculated	, horo		Axis						
	calculated	nere			0.4					
					0.3					
					0.2					
					0.1					
					0			-	-	
					0	0.2	0.4	0.6	0.8	1
							Axis	Title		

ally be filled
5 0.8 1
_

# Good Luck!