

Chapter 1- Uncertainties

Addition or subtraction:

$$f(x, y, z) = x + y + z \rightarrow \delta f(x, y, z) = \sqrt{\delta x^2 + \delta y^2 + \delta z^2}$$

Multiplication or division:

$$f(x, y, z) = \frac{xy}{z} \rightarrow \frac{\delta f}{|f|} = \sqrt{\left(\frac{\delta x}{|x|}\right)^2 + \left(\frac{\delta y}{|y|}\right)^2 + \left(\frac{\delta z}{|z|}\right)^2}$$

Multiplication or division by a constant (a):

$$f(x) = ax \rightarrow \delta f = a\delta x$$

Powers:

$$f(x) = x^n \rightarrow \frac{\delta f}{|f|} = |n| \frac{\delta x}{|x|}$$

Special functions:

$$1. f(x) = \sin(x) \rightarrow \delta f = \cos(x)\delta x$$

$$2. f(x) = e^x \rightarrow \delta f = e^x\delta x$$

$$3. f(x) = \ln(ax) \rightarrow \delta f = \frac{1}{|x|}\delta x$$

$$4. f(x) = \log_{10}(x) = \frac{\ln(x)}{\ln(10)} = \frac{1}{\ln(10)} \ln(x) = 0.43 \ln(x) \rightarrow \delta f = \frac{0.43}{|x|}\delta x$$

Average:

$$f(x) = \bar{x} \rightarrow \delta f = \sigma = \sqrt{\frac{1}{N-1} \sum_{i=1}^N (x_i - \bar{x})^2}$$

where σ is the standard deviation.

Standard error of the mean (if $N \geq 5$):

$$SE = \frac{\sigma}{\sqrt{N}}$$